

## VIBRATIONAL DYNAMICS OF THE H<sub>2</sub>O . HF COMPLEX. POTENTIAL ENERGY AND ELECTRIC DIPOLE MOMENT SURFACES

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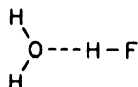
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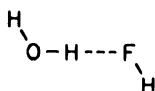
A total of 330 points on the potential energy and electric dipole moment surfaces of the ground electronic state of the H<sub>2</sub>O . HF complex have been calculated *ab initio* using the SCF method and many-body perturbation theory (MBPT). To keep the calculations manageable, the geometry parameters of H<sub>2</sub>O were fixed at their experimental values and only certain two-dimensional sections of the total surfaces have been evaluated. For each of the two-dimensional surface sections, analytic potential energy and electric dipole moment functions have been fitted through the points and corresponding vibration energy levels and effective electric dipole moments have been calculated using approximate vibrational Hamiltonians. The calculated values of resulting vibrational energies and effective electric dipoles form differently wide intervals for different vibrational modes. The intervals corresponding to the most interesting low frequency modes (out-of-plane and H<sub>2</sub>O vs HF stretching) are very narrow and coincide satisfactorily with the corresponding experimental values. A very reasonable agreement has also been obtained for the equilibrium geometry, electric dipole moment and dissociation energy  $D_e$  of the complex. These findings lead us to believe that the calculated potential energy and electric dipole moment surfaces are sufficiently accurate for predicting purposes and rationalization of the so far unassigned spectral data of H<sub>2</sub>O . HF.

The complex formed between one molecule of water and one of hydrogen fluoride, is the simplest possible hydrogen bonded complex in which water acts as the proton acceptor. For this reason it is of considerable chemical interest, and, not surprisingly, the subject of numerous experimental and theoretical studies throughout the years.

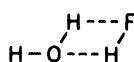
An early *ab initio* study of Kollman and Allen<sup>1</sup> has revealed that the complex may acquire four stable geometries



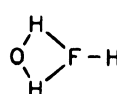
I



II



III



IV

Experimentally, the existence of the complex has been established through its microwave and infrared spectra<sup>2,3</sup>, and, only structure *I*, which is predicted to have the most favourable stabilization energy, has been found to be consistent with the spectra. In subsequent microwave studies<sup>4-12</sup> many properties of  $\text{H}_2\text{O} \cdot \text{HF}$  have been established quantitatively (e.g. geometry<sup>5</sup>, effective electric dipole moments<sup>8</sup>, effective potential energy function governing the out-of-plane bending mode<sup>6,9</sup>, dissociation energies<sup>12</sup>  $D_e$  and  $D_0$ ). Abundance of very precise experimental data has also stimulated activity of theorists<sup>13-21</sup>. Relative simplicity of  $\text{H}_2\text{O} \cdot \text{HF}$  has made it possible to apply sophisticated theoretical treatments and, after accounting for the electron correlation effects<sup>17-19</sup> (included via second- and third-order Møller–Plesset perturbation theory), the equilibrium geometries and electric dipoles and dissociation characteristics were obtained in an excellent agreement with available experimental information. Fairly less satisfactory agreement, however, was obtained for the vibrational frequencies which probe a much bigger portion of the potential energy surface of  $\text{H}_2\text{O} \cdot \text{HF}$ .

The reasons causing the failure of theory may be attributed to the fact that the vibrational analyses have been performed either in the harmonic approximation or within the frameworks of too-low-dimensional vibrational models. The aim of our effort is to overcome these limitations by accounting both for anharmonicity and the fact that certain vibrational motions of  $\text{H}_2\text{O} \cdot \text{HF}$  exhibit collective features.

The complex  $\text{H}_2\text{O} \cdot \text{HF}$  has nine independent vibrational degrees of freedom, some of which are related to strongly nonharmonic potentials. A complete theoretical study of this system, including the *ab initio* evaluation of the multi-dimensional potential energy and electric dipole moment surfaces and the solution of the complete dynamical vibrational problem, would thus represent an unfeasible task. Fortunately, since the vibrational frequencies of the  $\text{H}_2\text{O}$  and  $\text{HF}$  constituents are much higher than the frequencies of the intermolecular modes, the 9-dimensional dynamical problem can accurately be separated into two smaller problems (high and low frequency problems) by using the adiabatic approximation. Moreover, it appears that the same approximation may subsequently be used for similar separation of the intermolecular motions. To reduce the *ab initio* tedium, we keep the geometry parameters of  $\text{H}_2\text{O}$  at their experimental values and, with exception for the study of the interaction between the dissociation and  $\text{HF}$  stretching motions, we freeze the  $\text{HF}$  bond length at its equilibrium value in the complex. High quality of the adiabatic separation of the high (constituent) and low (intermolecular) frequency motions is a reliable guarantee for our assumption that the corresponding property surface sections should be highly parallel to the genuine ones. Secondly, we disregard from our *ab initio* calculations all the geometry configurations which are accessible only by more than two simultaneous vibrational displacements from the reference equilibrium configuration. Thirdly, we neglect completely the interactions between the  $\text{H}_2\text{O}$  and hydrogen bond bending motions possessing different

symmetries. The latter neglects seem to be justified reasonably by the preliminary results we have obtained with global electrostatic empirical potentials.

In this paper, we concentrate our attention to the evaluation of the property surfaces and their testing by comparing with the experimental equilibrium characteristics and dissociation asymptotics, and to the investigation of the intermode couplings by performing calculations of the vibrational energies and effective electric dipoles within the frameworks of one- and two-dimensional vibrational Hamiltonians pertaining to the evaluated property surface sections. A proper "fully-dimensional" evaluation of the vibrational characteristics is postponed for a future study.

## THEORETICAL

### *Coordinate System and Reference Configurations*

The previous experimental and theoretical studies have established that the equilibrium geometry of H<sub>2</sub>O . HF is pyramidal at the oxygen atom and that its hydrogen bond is slightly nonlinear. However, the height of the potential barrier to inversion through the planar C<sub>2v</sub> form of the complex is very low. Thus, to classify the vibration-rotation energy spectrum of the complex it is convenient to use the point group C<sub>2v</sub>. Accordingly, geometrical deformations of H<sub>2</sub>O . HF can conveniently be described relative to a reference configuration of C<sub>2v</sub> symmetry using the following symmetry coordinates (for definition of symbols see Fig. 1)

$$S_1(A_1) = R - R_c = \Delta R \quad (1a)$$

$$S_2(A_1) = \gamma - \gamma_c = \Delta\gamma \quad (1b)$$

$$S_3(A_1) = r - r_c = \Delta r \quad (1c)$$

$$S_4(A_1) = (d_{13} + d_{23} - 2 d_c)/\sqrt{2} \quad (1d)$$

$$S_5(B_1) = \alpha_i \quad (1e)$$

$$S_6(B_1) = \beta_i \quad (1f)$$

$$S_7(B_1) = (d_{13} - d_{23})/\sqrt{2} \quad (1g)$$

$$S_8(B_2) = \alpha_0 \quad (1h)$$

$$S_0(B_2) = \beta_0 \quad (1i)$$

Earlier *ab initio* calculations<sup>13,19</sup> have also revealed that the high frequency  $\nu_2$ ,  $\nu_4$ , and  $\nu_7$  vibrations of the complex are essentially almost the same as those of the isolated water molecule. The last high frequency motion, i.e. the HF stretching motion  $\nu_3$ , appears to be affected considerably more by complexation. Still, it is opposed by a very deep and narrow potential. Thus, from the point of view of the low frequency (intermolecular) vibrational motions, the  $\text{H}_2\text{O}$  and HF fragments may be treated, to a high degree of approximation, as rigid units. If doing that (by fixing the water geometry parameters at the values corresponding to the equilibrium geometry of the isolated water molecule and the HF bond length at its optimal value for the planar  $C_{2v}$  geometrically defined reference configuration), then, any actual configuration of  $\text{H}_2\text{O} \cdot \text{HF}$  can be described by the following components of the atomic position vectors of the Hougen–Bunker–Johns (HBJ) nonrigid reference configuration<sup>22</sup>

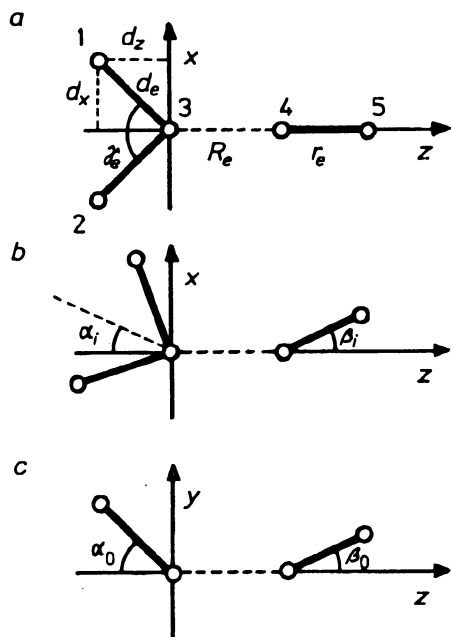


FIG. 1  
 Vibrational coordinates of  $\text{H}_2\text{O} \cdot \text{HF}$ : **a** rigid reference configuration ( $C_{2v}$ ), **b** in-plane bending coordinates, **c** out-of-plane bending coordinates

$$a_{1x} = d_x \cos\alpha_i + d_z \cos\alpha_0 \sin\alpha_i + D_x \quad (2a)$$

$$a_{1y} = a_{2y} = d_z \sin\alpha_0 + D_y \quad (2b)$$

$$a_{1z} = d_x \sin\alpha_i - d_z \cos\alpha_0 \cos\alpha_i + D_z \quad (2c)$$

$$a_{2x} = -d_x \cos\alpha_i + d_z \cos\alpha_0 \sin\alpha_i + D_x \quad (2d)$$

$$a_{2z} = -d_x \sin\alpha_i - d_z \cos\alpha_0 \cos\alpha_i + D_z \quad (2e)$$

$$a_{3x} = a_{4x} = D_x \quad (2f)$$

$$a_{3y} = a_{4y} = D_y \quad (2g)$$

$$a_{3z} = D_z \quad (2h)$$

$$a_{4z} = R_e + \Delta R + D_z \quad (2i)$$

$$a_{5x} = r_e \sin\beta_i \cos\beta_0 + D_x \quad (2j)$$

$$a_{5y} = r_e \sin\beta_0 + D_y \quad (2k)$$

$$a_{5z} = R_e + \Delta R + r_e \cos\beta_i \cos\beta_0 + D_z \quad (2l)$$

The mass dependent quantities  $D_x$ ,  $D_y$ ,  $D_z$  in Eqs (2) are defined so that it holds

$$\sum_i m_i a_{i\alpha} = 0 \quad (\alpha = x, y, z), \quad (3)$$

where  $m_i$  is the mass of the  $i$ -th atom.

The HBJ reference configuration exactly follows all the intermolecular large-amplitude displacements. Consequently, the H<sub>2</sub>O and HF vibrational displacements measured

with respect to this reference remain small and can be processed using the Cartesian displacement coordinates  $\mathbf{d}_i$  fulfilling the following constraints

$$\sum_i m_i \mathbf{d}_i = 0 \quad (4a)$$

$$\sum_i m_i [\mathbf{a}_i \times \mathbf{d}_i] = 0 \quad (4b)$$

$$\sum_i m_i \left( \frac{\partial \mathbf{a}_i}{\partial \rho_j} \right) \mathbf{d}_i = 0 \quad (\rho_j = \Delta R, \alpha_i, \alpha_0, \beta_i, \beta_0). \quad (4c)$$

### *Kinetic Energy Operator*

With the above definition of the molecule-fixed position vectors (2) for the HBJ reference configuration and the vibrational displacement coordinates  $\mathbf{d}_i$  the kinetic energy operator is obtained as

$$\mathbf{T} = \frac{1}{2} \mu^{1/4} \sum_{\alpha, \beta} (\mathbf{J}_\alpha - \mathbf{p}_\alpha) \mu_{\alpha\beta} \mu^{-1/2} (\mathbf{J}_\beta - \mathbf{p}_\beta) \mu^{1/4} + \frac{1}{2} \mu^{1/4} \sum_{ij} \mathbf{P}_i \mu^{-1/2} \mathbf{P}_j \mu^{1/4} \quad (5)$$

with  $\alpha, \beta = x, y, z, S_1, S_5, S_6, S_8, S_9$  and  $i, j = S_2, S_3, S_4, S_7$ .

All the quantities in Eq. (5) are formally defined by analogous relations as in ref.<sup>22</sup>.

The explicit expressions for the components of the inertia tensor  $I$  and its inverse  $\mu$  have been obtained with the aid of the computer algebra program MAPLE (see ref.<sup>23</sup>). Note that in deriving these terms, no attempt has been made to exclude or minimize any of the off-diagonal coupling terms in the  $\mu$  tensor.

### *Ab initio Calculations*

*Methods.* All calculations of the interaction potential in the  $\text{H}_2\text{O} \cdot \text{HF}$  complex have been carried out in what is known as the supermolecule model (see ref.<sup>24</sup>) and all results were afterwards corrected for the basis set superposition effect by using the counterpoise correction method<sup>24,25</sup>. To obtain the interaction potential  $V(R, r, \alpha_i, \alpha_0, \beta_i, \beta_0)$  in terms of the two-dimensional cross-sections, the point-wise calcu-

lations of the interaction energy have been carried out in several different approximations. We have employed the SCF HF method to obtain the electrostatic and inductive contributions to  $V$ , while the dispersion and intramolecular correlation effects have been accounted for at the level of the many-body perturbation theory (MBPT, see ref.<sup>26</sup>). The MBPT calculations of the electron correlation contribution have been performed at the level of the second-, third- and complete fourth-order approximations, which will be referred to as MBPT2, MBPT3, and MBPT4, respectively. We have also investigated the performance of the approximate fourth-order approach, referred to as the SDQ-MBPT4 method<sup>26</sup>.

The main features of the interaction potential are correctly predicted already at the SCF level of approximation. For the H<sub>2</sub>O and HF fragment geometries fixed at the experimental values of the free molecules, the optimal value of the H-bond distance,  $R(\text{OH})$ , acquires value 3.348 a.u. and the pertinent SCF interaction energy amounts to -12.466 mH; the corresponding experimental values are 3.267 a.u. and -11.4 mH, respectively. Including the electron correlation causes only small changes in both the equilibrium geometry and interaction energy. Moreover, in most cases different MBPT approaches lead to virtually same results. The mutual agreement between the results of the different MBPT approaches shows that the major part of the electron correlation contribution to the interaction potential is already recovered at the level of the MBPT2 approximation. The compatibility of different MBPT interaction potentials also supports our claim of a high accuracy of the interaction energies computed in this study.

*Basis set.* All calculations have been performed with the so-called polarized GTO/CGTO basis sets<sup>27,28</sup>. In order to avoid excessive basis set superposition contributions to the interaction energy, a series of high-quality GTO/CGTO basis sets for H, O and F has been generated following the method of refs<sup>27,28</sup>. The hydrogen polarized basis set of the form [11s6p/4s2p] has been derived by the polarization-oriented<sup>27,28</sup> extension of the (10s) GTO set of van Duijneveldt<sup>29</sup>. The same method<sup>27,28</sup> applied to the (13s8p) basis sets<sup>29</sup> for O and F has led to the [14s9p6d/6.4.2] polarized GTO/CGTO sets used in the present study. Those basis sets, by the method of their derivation, provide highly accurate results for the major electric properties (the dipole and quadrupole moments and dipole polarizabilities) of the isolated fragments. In this respect their quality is at least as high as that of the standard polarized basis sets<sup>27,28</sup>. However, in comparison with the standard polarized sets the present ones are more suitable for a simultaneous calculation of the geometry dependence of energy.

Another advantage of the extended polarized basis sets used in this study is that in comparison with the standard basis sets the size of the basis set superposition effects is considerably reduced at both the SCF and MBPT levels of approximation. In the vicinity of the complex equilibrium configuration the basis set superposition effect, as estimated by the counterpoise correction (refs<sup>24,25</sup>), amounts to about 0.5 mH for the SCF approximation and to about 2 mH for the MBPT2 approach. These numbers

should be referred to the non-corrected interaction energies of the order of  $-12$  mH and  $-14$  mH, respectively. In higher orders of the MBPT approach the additional basis set superposition contribution is virtually negligible; its dominant part is accounted for at the MBPT2 level of approximation. Moreover, since the size of the basis set superposition effect at the most significant complex geometries does not exceed about 10 per cent of the total interaction energy, the use of the counterpoise correction appears to be reasonably justified<sup>31</sup>.

The details of the extended polarized GTO/CGTO basis sets employed in this study are available from one of the authors (A. J. S.).

*Computational details.* In all calculations the geometry parameters of the water molecule has been kept fixed at the corresponding experimental values:  $R(\text{OH}) = 1.81117$  a.u.,  $\angle \text{HOH} = 104.44^\circ$ . All other geometry parameters of the complex have been varied in a pair-wise way leading to two-dimensional cross-sections of the total interaction surface. At both the SCF and MBPT levels of approximation the *s*-components of the cartesian GTO/CGTO's have been removed from the molecular basis set. Moreover, in MBPT calculations no excitations were allowed from the 1s core orbitals of F and O. The calculations have been carried out by using the MOLCAS system of quantum chemistry programs<sup>32–35</sup>.

*Dipole moment surfaces.* Along with the interaction energy surface we have also evaluated the electric dipole moment surface. Some pilot calculations have been carried out at the MBPT4 approximation by using the appropriate finite field perturbation approach<sup>37</sup>. It has been found that the MBPT4 dipole moment surfaces are essentially parallel to those obtained at the level of the SCF approximation. Thus, the interaction dipole surface can be obtained with a good accuracy from much less expensive SCF treatment based on the Hellmann–Feynman theorem. The absolute values of the dipole moments can be then obtained by simply adding the dipole moments of HF and H<sub>2</sub>O computed within a high-level correlated approximation. Accordingly, the total electric dipole moment surface,  $\mathbf{m}^{\text{corr}}$ , is constructed as the following sum

$$\mathbf{m}^{\text{corr}} = \mathbf{m}^{\text{SCF}} + \Delta\mathbf{m}_{\text{H}_2\text{O}}^{\text{corr}} + \Delta\mathbf{m}_{\text{HF}}^{\text{corr}}, \quad (6)$$

where

$$\Delta\mathbf{m}_{\text{H}_2\text{O}}^{\text{corr}} = \mathbf{m}_{\text{H}_2\text{O}}^{\text{SDQ4}} - \mathbf{m}_{\text{H}_2\text{O}}^{\text{SCF}} \quad (7a)$$

and

$$\Delta\mathbf{m}_{\text{HF}}^{\text{corr}} = \mathbf{m}_{\text{HF}}^{\text{SDQ4}} - \mathbf{m}_{\text{HF}}^{\text{SCF}}. \quad (7b)$$



It is also worthwhile to mention that the dipole moment surface is virtually unaffected by the basis set superposition<sup>38</sup>. This is an additional advantage of the polarized basis sets used in the present study.

## RESULTS AND DISCUSSION

### *Potential Energy and Electric Dipole Moment Surfaces*

A total of 330 points were calculated covering an energy range up to approximately 13 000 cm<sup>-1</sup> above equilibrium. This set of points was chosen in order to sample the full range of values of the intermolecular vibrational coordinates and the HF stretching coordinate and to probe, in full details, the following two-dimensional cross-sections of the total property surfaces:  $R$  vs  $r$ ,  $R$  vs  $\alpha_i$ ,  $R$  vs  $\alpha_0$ ,  $R$  vs  $\beta_i$ ,  $R$  vs  $\beta_0$ ,  $\alpha_i$  vs  $\beta_i$ ,  $\alpha_0$  vs  $\beta_0$ ,  $\alpha_0$  vs  $\beta_i$ ,  $\alpha_i$  vs  $\alpha_0$ . No calculations were performed for the remaining  $\alpha_i$  vs  $\beta_0$  and  $\beta_i$  vs  $\beta_0$  interactions as they have been found, within the framework of our preliminary analysis based on the Buckingham and Fowler electrostatic model<sup>39</sup>, to be rather unimportant. The geometries and the energies and electric dipole moments of all the calculated points are collected in Table I.

For each of the calculated two-dimensional surface cross-sections,  $P_{ij}$ , analytic potential energy and electric dipole moment functions have been fitted through the corresponding points using the following power series

$$P_{ij} = \sum_{k,l} p_{kl}^{(ij)} x^k y^l \quad (ij = R, r, \alpha_i, \alpha_0, \beta_i, \beta_0), \quad (8)$$

where  $x$  and  $y$  are  $\exp(-\Delta R)$ ,  $\Delta r$ ,  $\alpha_i$ ,  $\alpha_0$ ,  $\beta_i$  and  $\beta_0$  for the potential energy functions, and  $x$  and  $y$  are  $R$ ,  $r$ ,  $\alpha_i$ ,  $\alpha_0$ ,  $\beta_i$  and  $\beta_0$  for the electric dipole moment functions.

The functional form (8) has turned out to be flexible enough to permit a practically quantitative fit of all the points. The expansion coefficients are available from the authors (O. B. and V. Š.). The fitted equilibrium and reference geometry parameters are collected in Table II. Typical representatives for the fitted functions are illustrated by Fig. 2.

### *Vibration Energies and Effective Electric Dipole Moments*

To evaluate the vibration energies  $E$  and eigenfunctions  $\Psi_k$  for each of the two-dimensional problem it is necessary to solve the corresponding two-dimensional Schrödinger equation

$$H^{(ij)} \Psi_k = E_k^{(ij)} \Psi_k \quad (ij = R, r, \alpha_i, \alpha_0, \beta_i, \beta_0), \quad (9)$$

TABLE I  
*Ab initio* MBPT4-SDQ energies and SCF dipole moment functions ( $E$ ,  $m_x$ ,  $m_y$ ,  $m_z$ ,  $R$ ,  $r$  in a.u.,  $\alpha_0$ ,  $\alpha_i$ ,  $\beta_0$ ,  $\beta_i$  in deg)

$R$	$r$	$E + 176$	$m_z$	$R$	$r$	$E + 176$	$m_z$
2.500	1.533	-.56649	-1.847	3.500	2.033	-.59760	-2.009
2.500	1.633	-.58638	-1.949	3.500	2.133	-.58733	-2.084
2.500	1.683	-.59248	-2.001	3.500	2.233	-.57593	-2.162
2.500	1.708	-.59475	-2.028	3.500	2.333	-.56392	-2.242
2.500	1.733	-.59658	-2.054	3.519	1.639	-.60803	-1.734
2.500	1.758	-.59799	-2.081	3.538	1.882	-.60914	-1.892
2.500	1.783	-.59902	-2.109	3.594	1.564	-.59864	-1.678
2.500	1.833	-.60008	-2.164	3.750	1.733	-.61214	-1.759
2.500	1.933	-.59897	-2.276	4.000	1.533	-.59225	-1.618
2.500	2.033	-.59471	-2.392	4.000	1.633	-.60644	-1.671
2.500	2.133	-.58834	-2.510	4.000	1.683	-.60979	-1.699
2.500	2.233	-.58059	-2.630	4.000	1.708	-.61072	-1.712
2.500	2.333	-.57196	-2.753	4.000	1.733	-.61120	-1.726
2.500	2.433	-.56282	-2.877	4.000	1.758	-.61129	-1.741
2.500	2.533	-.55344	-3.002	4.000	1.783	-.61102	-1.755
2.750	1.733	-.60630	-1.972	4.000	1.833	-.60953	-1.784
3.000	1.533	-.58821	-1.745	4.000	1.933	-.60341	-1.843
3.000	1.633	-.60427	-1.822	4.000	2.033	-.59463	-1.905
3.000	1.683	-.60854	-1.862	4.000	2.133	-.58391	-1.969
3.000	1.708	-.60992	-1.883	4.000	2.233	-.57209	-2.034
3.000	1.733	-.61086	-1.903	4.500	1.733	-.60916	-1.677
3.000	1.758	-.61140	-1.924	5.000	1.533	-.58906	-1.552
3.000	1.783	-.61158	-1.945	5.000	1.633	-.60294	-1.597
3.000	1.833	-.61097	-1.988	5.000	1.683	-.60614	-1.620
3.000	1.933	-.60667	-2.075	5.000	1.708	-.60698	-1.632
3.000	2.033	-.59943	-2.166	5.000	1.733	-.60740	-1.643
3.000	2.133	-.59028	-2.260	5.000	1.758	-.60741	-1.655
3.000	2.233	-.57994	-2.357	5.000	1.783	-.60706	-1.667
3.000	2.333	-.56891	-2.456	5.000	1.833	-.60542	-1.692
3.000	2.433	-.55756	-2.558	5.000	1.933	-.59910	-1.741
3.239	1.919	-.60774	-1.991	5.000	2.033	-.58993	-1.793
3.250	1.733	-.61257	-1.846	5.000	2.133	-.57894	-1.845
3.295	1.639	-.60760	-1.770	6.000	1.533	-.58686	-1.516
3.295	1.863	-.61071	-1.933	6.000	1.633	-.60066	-1.558
3.332	1.676	-.61053	-1.789	6.000	1.683	-.60381	-1.580
3.407	1.751	-.61302	-1.827	6.000	1.708	-.60463	-1.591
3.482	1.826	-.61184	-1.864	6.000	1.733	-.60502	-1.602
3.500	1.533	-.59277	-1.671	6.000	1.758	-.60501	-1.613
3.500	1.633	-.60747	-1.733	6.000	1.783	-.60464	-1.624
3.500	1.683	-.61107	-1.765	6.000	1.833	-.60295	-1.647
3.500	1.708	-.61212	-1.782	6.000	1.933	-.59655	-1.693
3.500	1.733	-.61274	-1.798	6.000	2.033	-.58730	-1.741
3.500	1.758	-.61295	-1.815	7.000	1.733	-.60370	-1.579
3.500	1.783	-.61280	-1.831	10.00	1.733	-.60216	-1.552
3.500	1.833	-.61156	-1.866	15.00	1.733	-.60156	-1.541
3.500	1.933	-.60602	-1.936				

TABLE I  
(Continued)

<i>R</i>	$\alpha_0$	<i>E</i> + 176	<i>m<sub>y</sub></i>	<i>m<sub>z</sub></i>	<i>R</i>	$\alpha_i$	<i>E</i> + 176	<i>m<sub>x</sub></i>	<i>m<sub>z</sub></i>
2.500	0	-.59822	.000	-2.087	3.376	50	-.60586	.584	-1.515
2.500	10	-.59831	.146	-2.075	4.000	10	-.61107	.133	-1.730
2.500	20	-.59853	.288	-2.039	4.000	20	-.61049	.262	-1.690
2.500	40	-.59931	.533	-1.906	4.000	30	-.60952	.383	-1.625
2.500	60	-.59828	.713	-1.681	4.000	50	-.60641	.587	-1.430
2.500	80	-.59493	.797	-1.403	5.000	10	-.60725	.134	-1.645
2.500	100	-.58710	.781	-1.095	5.000	20	-.60691	.264	-1.607
3.000	0	-.61147	.000	-1.928	5.000	30	-.60634	.386	-1.545
3.000	10	-.61154	.142	-1.916	5.000	50	-.60456	.590	-1.359
3.000	20	-.61172	.280	-1.881					
3.000	40	-.61211	.523	-1.745					
3.000	60	-.61179	.699	-1.531					
3.000	80	-.60970	.785	-1.260					
3.000	100	-.60476	.773	-0.962					
3.376	0	-.61306	.000	-1.842					
3.376	10	-.61312	.140	-1.830					
3.376	20	-.61326	.276	-1.795					
3.376	40	-.61356	.516	-1.660					
3.376	60	-.61334	.691	-1.448					
3.376	80	-.61178	.779	-1.181					
3.376	100	-.60813	.770	-0.888					
4.000	0	-.61127	.000	-1.743					
4.000	10	-.61130	.138	-1.732					
4.000	20	-.61137	.271	-1.697					
4.000	40	-.61154	.509	-1.562					
4.000	60	-.61134	.684	-1.352					
4.000	80	-.61026	.773	-1.088					
4.000	100	-.60785	.767	-0.802					
5.000	0	-.60737	.000	-1.658					
5.000	10	-.60738	.136	-1.646					
5.000	20	-.60740	.268	-1.611					
5.000	40	-.60740	.504	-1.475					
5.000	60	-.60717	.678	-1.266					
5.000	80	-.60643	.769	-1.005					
5.000	100	-.60498	.765	-0.725					
<i>R</i>	$\alpha_i$	<i>E</i> + 176	<i>m<sub>x</sub></i>	<i>m<sub>z</sub></i>	<i>R</i>	$\beta_0$	<i>E</i> + 176	<i>m<sub>y</sub></i>	<i>m<sub>z</sub></i>
2.500	10	-.59773	.127	-2.072	2.500	10	-.59736	-.149	-2.07
2.500	20	-.59625	.253	-2.027	2.500	20	-.59469	-.294	-2.02
2.500	30	-.59369	.372	-1.954	2.500	30	-.58990	-.427	-1.94
2.500	50	-.58444	.579	-1.738	2.500	50	-.57103	-.641	-1.70
3.000	10	-.61111	.130	-1.914	2.500	80	-.48585	-.750	-1.15
3.000	20	-.61005	.257	-1.871	3.000	10	-.61104	-.140	-1.91
3.000	30	-.60826	.377	-1.801	3.000	20	-.60972	-.275	-1.86
3.000	50	-.60210	.582	-1.592	3.000	30	-.60737	-.401	-1.79
3.376	10	-.61278	.132	-1.827	3.000	50	-.59835	-.604	-1.57
3.376	20	-.61194	.260	-1.786	3.000	80	-.55877	-.730	-1.09
3.376	30	-.61054	.380	-1.718	3.376	10	-.61280	-.136	-1.82
					3.376	20	-.61199	-.268	-1.78
					3.376	30	-.61058	-.390	-1.71
					3.376	50	-.60525	-.591	-1.50
					3.376	80	-.58297	-.726	-1.05
					4.000	10	-.61114	-.133	-1.73
					4.000	20	-.61074	-.262	-1.69
					4.000	30	-.61005	-.383	-1.62
					4.000	50	-.60759	-.582	-1.43
					4.000	80	-.59845	-.729	-1.01
					5.000	10	-.60731	-.132	-1.64
					5.000	20	-.60713	-.261	-1.60
					5.000	30	-.60683	-.381	-1.54
					5.000	50	-.60581	-.581	-1.36
					5.000	80	-.60280	-.737	-0.97
<i>R</i>	$\beta_i$	<i>E</i> + 176	<i>m<sub>x</sub></i>	<i>m<sub>z</sub></i>	<i>R</i>	$\beta_i$	<i>E</i> + 176	<i>m<sub>x</sub></i>	<i>m<sub>z</sub></i>
2.500	10	-.59744	-.151	-2.07	2.500	10	-.59744	-.151	-2.07
2.500	20	-.59503	-.296	-2.02	2.500	20	-.59503	-.296	-2.02
2.500	30	-.59072	-.431	-1.94	2.500	30	-.59072	-.431	-1.94
2.500	50	-.57379	-.647	-1.69	2.500	50	-.57379	-.647	-1.69
2.500	80	-.49677	-.749	-1.12	2.500	80	-.49677	-.749	-1.12
3.000	10	-.61108	-.141	-1.91	3.000	10	-.61108	-.141	-1.91
3.000	20	-.60988	-.278	-1.86	3.000	20	-.60988	-.278	-1.86
3.000	30	-.60777	-.404	-1.79	3.000	30	-.60777	-.404	-1.79
3.000	50	-.59964	-.611	-1.57	3.000	50	-.59964	-.611	-1.57

TABLE I  
(Continued)

$R$	$\beta_i$	$E + 176$	$m_x$	$m_z$	$\alpha_0$	$\beta_0$	$E + 176$	$m_y$	$m_z$
3.000	80	-.56383	-.743	-1.074	45	-80	-.58262	1.283	-.840
3.376	10	-.61283	-.137	-1.827	45	-50	-.60503	1.155	-1.287
3.376	20	-.61210	-.270	-1.785	45	-30	-.61066	.957	-1.493
3.376	30	-.61082	-.394	-1.716	45	-20	-.61224	.836	-1.561
3.376	50	-.60604	-.597	-1.505	45	-10	-.61319	.704	-1.601
3.376	80	-.58592	-.739	-1.045	45	10	-.61343	.430	-1.597
4.000	10	-.61115	-.134	-1.730	45	20	-.61270	.298	-1.553
4.000	20	-.61079	-.264	-1.691	45	30	-.61132	.174	-1.481
4.000	30	-.61018	-.385	-1.626	45	50	-.60586	-.030	-1.265
4.000	50	-.60798	-.586	-1.430	45	80	-.58197	-.176	-.798
4.000	80	-.59975	-.738	-1.010	60	-80	-.58056	1.401	-.677
5.000	10	-.60731	-.132	-1.645	60	-50	-.60386	1.277	-1.123
5.000	20	-.60715	-.261	-1.608	60	-30	-.60990	1.080	-1.329
5.000	30	-.60688	-.381	-1.547	60	-20	-.61165	.959	-1.396
5.000	50	-.60597	-.582	-1.363	60	-10	-.61278	.828	-1.436
5.000	80	-.60323	-.741	-.972	60	10	-.61334	.554	-1.431
					60	20	-.61277	.422	-1.386
					60	30	-.61154	.297	-1.314
					60	50	-.60635	.092	-1.095
					60	80	-.58248	-.056	-.623
					80	-80	-.57608	1.476	-.417
					80	-50	-.60079	1.357	-.859
					80	-30	-.60745	1.164	-1.063
					80	-20	-.60950	1.044	-1.130
					80	-10	-.61092	.914	-1.169
					80	10	-.61210	.643	-1.163
					80	20	-.61184	.511	-1.118
					80	30	-.61095	.387	-1.045
					80	50	-.60644	.182	-.824
					80	80	-.58299	.033	-.346
					100	-80	-.56994	1.447	-1.138
					100	-50	-.59575	1.336	-.572
					100	-30	-.60294	1.148	-.773
					100	-20	-.60526	1.031	-.838
					100	-10	-.60696	.903	-.877
					100	10	-.60879	.636	-.870
					100	20	-.60890	.506	-.824
					100	30	-.60841	.384	-.751
					100	50	-.60474	.183	-.529
					100	80	-.58149	.042	-.045
$\alpha_0$	$\beta_0$	$E + 176$	$m_y$	$m_z$	$\alpha_i$	$\beta_i$	$E + 176$	$m_x$	$m_z$
10	-80	-.58340	.864	-1.049	10	-80	-.58325	.865	-1.037
10	-50	-.60537	.730	-1.499	10	-50	-.60446	.726	-1.493
10	-30	-.61065	.530	-1.707	10	-30	-.60979	.524	-1.703
10	-20	-.61206	.408	-1.775	10	-20	-.61132	.401	-1.771
10	-10	-.61286	.276	-1.816	10	-10	-.61229	.269	-1.813
10	10	-.61285	.003	-1.815	10	10	-.61280	-.005	-1.813
10	20	-.61203	-.128	-1.773					
10	30	-.61059	-.251	-1.704					
10	50	-.60519	-.452	-1.493					
10	80	-.58250	-.589	-1.039					
20	-80	-.58363	.997	-1.017					
20	-50	-.60547	.865	-1.466					
20	-30	-.61075	.666	-1.673					
20	-20	-.61217	.544	-1.741					
20	-10	-.61299	.412	-1.782					
20	10	-.61299	.139	-1.780					
20	20	-.61217	.007	-1.737					
20	30	-.61072	-.115	-1.667					
20	50	-.60524	-.317	-1.455					
20	80	-.58210	-.457	-.998					
40	-80	-.58305	1.233	-.886					
40	-50	-.60524	1.104	-1.333					
40	-30	-.61077	.906	-1.540					
40	-20	-.61230	.784	-1.607					
40	-10	-.61321	.652	-1.647					
40	10	-.61337	.379	-1.644					
40	20	-.61260	.246	-1.600					
40	30	-.61119	.122	-1.529					
40	50	-.60569	-.081	-1.313					
40	80	-.58188	-.225	-.848					

TABLE I  
(Continued)

$\alpha_i$	$\beta_i$	$E + 176$	$m_x$	$m_z$	$\alpha_i$	$\beta_i$	$E + 176$	$m_x$	$m_z$	
10	-80	-.58325	.865	-1.037	50	-10	-.60460	.716	-1.504	
10	-50	-.60446	.726	-1.493	50	10	-.60678	.451	-1.499	
10	-30	-.60979	.524	-1.703	50	20	-.60735	.321	-1.455	
10	-20	-.61132	.401	-1.771	50	30	-.60751	.201	-1.383	
10	-10	-.61229	.269	-1.813	50	50	-.60597	.001	-1.166	
10	10	-.61280	-.005	-1.813	50	80	-.58868	-.135	-.673	
10	20	-.61234	-.138	-1.771						
10	30	-.61135	-.262	-1.701	$\bar{\alpha}_0^a$	$\bar{\alpha}_i^a$	$E + 176$	$m_x$	$m_y$	$m_z$
10	50	-.60721	-.466	-1.489						
10	80	-.58832	-.612	-1.027	10	10	-.61284	.132	.138	-1.816
20	-80	-.58057	.984	-1.004	20	10	-.61300	.132	.272	-1.782
20	-50	-.60253	.849	-1.454	40	10	-.61337	.133	.509	-1.649
20	-30	-.60828	.650	-1.662	60	10	-.61323	.134	.681	-1.441
20	-20	-.61002	.528	-1.730	80	10	-.61175	.135	.767	-1.178
20	-10	-.61122	.396	-1.772	100	10	-.60815	.137	.758	-0.890
20	10	-.61222	.123	-1.771	10	20	-.61202	.260	.132	-1.775
20	20	-.61203	-.009	-1.729	20	20	-.61223	.260	.260	-1.743
20	30	-.61135	-.132	-1.659	40	20	-.61279	.262	.487	-1.618
20	50	-.60790	-.337	-1.447	60	20	-.61289	.265	.651	-1.421
20	80	-.59016	-.485	-.982	80	20	-.61165	.267	.733	-1.172
30	-80	-.57800	1.094	-.947	100	20	-.60821	.270	.722	-0.896
30	-50	-.60030	.964	-1.391	10	30	-.61065	.380	.123	-1.708
30	-30	-.60632	.767	-1.596	20	30	-.61095	.381	.242	-1.680
30	-20	-.60822	.646	-1.664	40	30	-.61182	.384	.452	-1.567
30	-10	-.60961	.516	-1.704	60	30	-.61233	.387	.603	-1.389
30	10	-.61106	.244	-1.703	80	30	-.61149	.391	.676	-1.161
30	20	-.61114	.112	-1.660	100	30	-.60830	.395	.665	-0.907
30	30	-.61076	-.010	-1.591	10	50	-.60609	.584	.094	-1.509
30	50	-.60803	-.214	-1.378	20	50	-.60671	.585	.185	-1.490
30	80	-.59112	-.362	-.909	40	50	-.60870	.589	.344	-1.415
50	-80	-.57312	1.271	-.774	60	50	-.61060	.595	.455	-1.292
50	-50	-.59479	1.151	-1.202	80	50	-.61102	.600	.505	-1.128
50	-30	-.60090	.961	-1.400	100	50	-.60861	.605	.490	-0.939
50	-20	-.60297	.843	-1.465						

<sup>a</sup>  $\bar{\alpha}_0, \bar{\alpha}_i$  satisfy the following relations:

$$\alpha_0 = \arccos \frac{\cos \bar{\alpha}_0 \cos \bar{\alpha}_i}{\sqrt{1 - \cos^2 \bar{\alpha}_0 \cos^2 \bar{\alpha}_i}}$$

$$\alpha_i = \arcsin (\cos \bar{\alpha}_0 \sin \bar{\alpha}_i) .$$

where the Hamiltonians  $\mathbf{H}^{(ij)}$  may be written as<sup>22</sup>

$$\mathbf{H}^{(ij)} = \frac{1}{2} \sum_{ij} \mu_{ij}^0 \mathbf{J}_i \mathbf{J}_j + V_{ij} + H_{\text{hot}}^{(ij)}, \quad (10)$$

where  $\mu_{ij}^0$  are the zeroth-order reduced masses,  $\mathbf{J}_k$  the pertinent momenta,  $V_{ij}$  the pertinent potential energy functions and  $H_{\text{hot}}^{(ij)}$  higher order energy terms. The higher order terms  $H_{\text{hot}}^{(ij)}$  contain energies comparable to the contributions corresponding to the neglected intermode interactions. Hence, we have decided to neglect them and postpone

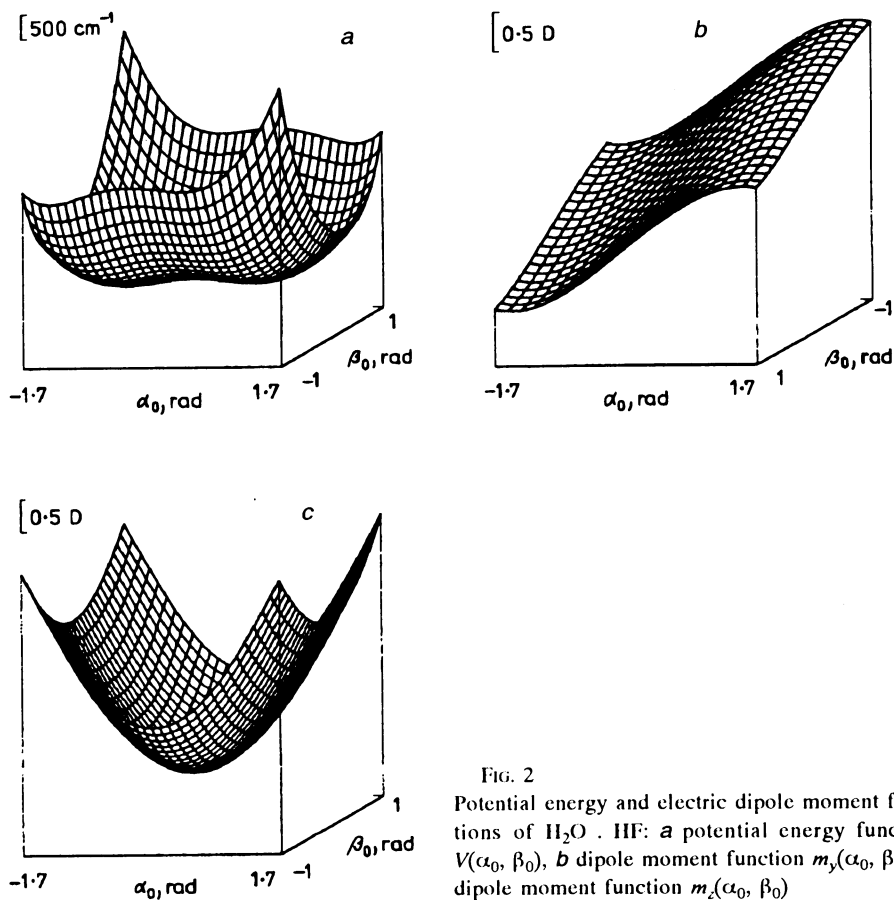


FIG. 2  
Potential energy and electric dipole moment functions of  $\text{H}_2\text{O}$ . HF: **a** potential energy function  $V(\alpha_0, \beta_0)$ , **b** dipole moment function  $m_y(\alpha_0, \beta_0)$ , **c** dipole moment function  $m_z(\alpha_0, \beta_0)$

their respecting for a future study which will be devoted to a fully-dimensional study of the discussed problem.

The approximate eigen-characteristics have been obtained variationally by diagonalizing the simplified Hamiltonians ( $\hat{H}$ ) as matrices over basis set functions expressed as products  $\Phi_i(v_i) \Phi_j(v_j)$ . The functions  $\Phi_i(v_i)$  and  $\Phi_j(v_j)$  were obtained numerically by solving the corresponding uncoupled one-dimensional Schrödinger equations. The lowest energies evaluated in this way are collected in Table III.

TABLE II  
The geometry parameters<sup>a</sup> and dissociation energy of the H<sub>2</sub>O . HF complex

$R_{OF}$ , Å	$r$ , Å	$d$ , Å	$\gamma_0$ , deg	$\alpha_0$ , deg	$D_e$ , kcal mol <sup>-1</sup>	Origin
Equilibrium C <sub>s</sub> geometry						
2.704	0.933 <sup>b</sup>	0.958 <sup>b</sup>	104.44 <sup>b</sup>	45.5	7.78	This paper
2.642	0.935	0.960	105.0	52.1		Ref. <sup>19</sup>
2.662				46.0	7.2	Experiment <sup>3,6</sup>
Planar C <sub>2v</sub> geometry						
2.719	0.933	0.958 <sup>b</sup>	104.44 <sup>b</sup>	0.0 <sup>b</sup>		This paper

<sup>a</sup> See Fig. 1; <sup>b</sup> held fixed.

TABLE III  
The vibrational frequencies of the H<sub>2</sub>O . HF complex (in cm<sup>-1</sup>) obtained with one- and two-dimensional models

Mode	1-D	2-D Calculations	Experiment <sup>a</sup>
$\nu_1(R)$	200	204( $\alpha_0$ ), 196( $\alpha_i$ ), 189( $\beta_0$ ), 189( $\beta_i$ ), 205( $r$ )	176 ± 15
$\nu_3(r)$	3 661	3 660( $R$ )	3 608 ± 2
$\nu_5(\alpha_i)$	357	350( $R$ ), 197( $\beta_i$ ), 378( $\alpha_0$ )	157 ± 10
2 $\nu_5(\alpha_i)$	715	696( $R$ ), 394( $\beta_i$ ), 756( $\alpha_0$ )	330 ± 30
$\nu_6(\beta_i)$	587	540( $R$ ), 733( $\alpha_i$ )	696 ± 30
$\nu_8(\alpha_0)$	82	83( $R$ ), 70( $\beta_0$ ), 92( $\alpha_i$ )	64 ± 10
2 $\nu_8(\alpha_0)$	283	283( $R$ ), 229( $\beta_0$ ), 294( $\alpha_i$ )	267 ± 35
$\nu_9(\beta_0)$	617	567( $R$ ), 645( $\alpha_0$ )	666 ± 30

<sup>a</sup> Refs<sup>3,6</sup>.

The effective electric dipole moments,  $\langle \mathbf{m}(v_i, v_j) \rangle$ , have been evaluated as the following averages

$$\langle \mathbf{m}(v_i, v_j) \rangle = \langle v_i v_j | \mathbf{m}_{ij} | v_i v_j \rangle. \quad (11)$$

The values of these effective constants of the lowest vibrational states are given in Table IV.

A brief inspection of Table III reveals that in addition to the three water vibrational motions the H<sub>2</sub>O . HF complex possesses three more rather characteristic motions. Namely the H<sub>2</sub>O vs HF and HF stretching and the H<sub>2</sub>O out-of-plane bending motions. The energies corresponding to the remaining bending motions exhibit very strong model dependences indicating thus their collective behaviour. Especially the interaction between the  $\alpha_i$  and  $\beta_i$  bending motions appears to be of crucial importance as its respecting shifts the only "really improperly" behaving  $\alpha_i$  and  $\beta_i$  energies in the proper direction. In any case, the calculated energies are in a much closer agreement with experimental values than those which are available from the previous *ab initio* studies (compare Tables III and V). A similar conclusions can also be derived from inspection of the Table IV comprising the effective electric dipole moments. The failure of the

TABLE IV

The effective electric dipole moments of the H<sub>2</sub>O . HF complex (in Debye) obtained with two-dimensional models

State <sup>a</sup>  1,3,5,6,8,9⟩	$\langle \mathbf{m}(v_1, v_3, v_5, v_6, v_8, v_9) \rangle$	Experiment <sup>b</sup>
0 0 0 0 0 0	4.082( <i>Rα</i> <sub>0</sub> ), 4.352( <i>Rα</i> <sub>i</sub> ), 4.297( <i>Rβ</i> <sub>0</sub> ), 4.073 ±	
0.007	4.293( <i>Rβ</i> <sub>i</sub> ), 4.526( <i>Rr</i> ), 4.019( <i>α</i> <sub>0</sub> <i>β</i> <sub>0</sub> ), 4.293( <i>α</i> <sub>i</sub> <i>β</i> <sub>i</sub> ), 4.079( <i>α</i> <sub>0</sub> <i>α</i> <sub>i</sub> )	
1 0 0 0 0 0	4.056( <i>Rα</i> <sub>0</sub> ), 4.320( <i>Rα</i> <sub>i</sub> ), 4.262( <i>Rβ</i> <sub>0</sub> ), 3.91 ± 0.04 4.258( <i>Rβ</i> <sub>0</sub> ), 4.488( <i>Rr</i> )	
0 1 0 0 0 0	4.780( <i>Rr</i> )	
0 0 1 0 0 0	4.238( <i>Rα</i> <sub>i</sub> ), 4.189( <i>α</i> <sub>i</sub> <i>β</i> <sub>i</sub> ), 4.044( <i>α</i> <sub>0</sub> <i>α</i> <sub>i</sub> )	4.074 ± 0.016
0 0 0 1 0 0	4.059( <i>Rβ</i> <sub>i</sub> ), 4.146( <i>α</i> <sub>i</sub> <i>β</i> <sub>i</sub> )	
0 0 0 0 1 0	3.815( <i>Rα</i> <sub>0</sub> ), 3.756( <i>α</i> <sub>0</sub> <i>β</i> <sub>0</sub> ), 3.817( <i>α</i> <sub>0</sub> <i>α</i> <sub>i</sub> )	3.802 ± 0.007
0 0 0 0 0 1	4.068( <i>Rβ</i> <sub>0</sub> ), 3.944( <i>α</i> <sub>0</sub> <i>β</i> <sub>0</sub> )	
0 0 0 0 2 0	3.764( <i>Rα</i> <sub>0</sub> ), 3.693( <i>α</i> <sub>0</sub> <i>β</i> <sub>0</sub> ), 3.754( <i>α</i> <sub>0</sub> <i>α</i> <sub>i</sub> )	
0 0 1 0 1 0	3.798( <i>α</i> <sub>0</sub> <i>α</i> <sub>i</sub> )	3.76 ± 0.04



theory in describing the variation of the dipole moment with the H<sub>2</sub>O vs HF stretching excitation may be attributed to the rotational-vibrational interactions which are completely neglected in this study.

## CONCLUSIONS

Molecular potential energy and electric dipole moment surfaces of the H<sub>2</sub>O . HF complex have been probed by performing highly accurate *ab initio* calculations for all the two-dimensional cross-sections of these surfaces which are important for description of the complexation dynamics. From these data, approximate vibrational energies and effective electric dipole moments have been evaluated using approximate two-dimensional HBJ vibrational Hamiltonians. A comparison of these quantities with available experimental data has revealed that the present theory closely describes both the highest-frequency motion of the HF fragment and the lowest-frequency H<sub>2</sub>O vs HF stretching and H<sub>2</sub>O out-of-plane bending motions. The characteristics corresponding to the medium-frequency bending motions, however, exhibit strong model dependences indicating thus unusually strong inter-mode kinematic interactions. Nevertheless, the quantities vary within the intervals which are in accord with the present assignment of the experimental data. Moreover, the evaluated static characteristics (equilibrium geometry, equilibrium dipole moment, dissociation energy) seem to be in a close harmony with their experimental counterparts. Hence, we believe that the present property surfaces are very reliable approximations to the genuine ones and that might be useful for unambiguous experimental identifications of the so far unassigned transitions and for rationalization of yet unprobed properties of the H<sub>2</sub>O . HF complex.

TABLE V

Literature data on the calculated vibrational frequencies of the H<sub>2</sub>O . HF complex (in cm<sup>-1</sup>)

Mode	Ref. <sup>13</sup>	Ref. <sup>16</sup>	Ref. <sup>19</sup>	Ref. <sup>17</sup>	Ref. <sup>20</sup>	Experiment
$\nu_1$	254	247	270	236	223	176 <sup>a</sup> , 180 <sup>a</sup>
$\nu_3$	3 599	3 858	3 791	3 764	4 250	3 608 <sup>b</sup>
$\nu_5$	250		252		223	157 <sup>a</sup> , 170 <sup>b</sup>
$\nu_6$	913		862		793	696 <sup>b</sup>
$\nu_8$	265		232	96	168	70 <sup>c</sup> , 64 <sup>a</sup>
2 $\nu_8$				255		267 <sup>a</sup>
$\nu_9$	740		742		656	666 <sup>b</sup>

<sup>a</sup> Ref.<sup>6</sup>; <sup>b</sup> ref.<sup>3</sup>; <sup>c</sup> ref.<sup>9</sup>.

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